Simpson's Paradox
NAME:
Does smoking improve survival?
(source: www.whfreeman.com/scc/content/eesee)
A survey concerned with thyroid and heart disease was conducted in 1972-74 in a district near Newcastle, UK by Tunbridge et al (1977). A follow-up study of the same subjects was conducted twenty years later by Vanderpump et al (1996). Here we explore data from the survey on the smoking habits of 1314 women who were classified as being a current smoker or as never having smoked at the time of the original survey. Of interest is whether or not they survived until the second survey.

Table 1: Relationship between smoking habits and 20-year survival

|  | Smoking status |  |
| :---: | :---: | :---: |
| Survival status | Yes | No |
| Dead | 139 | 230 |
| Alive | 443 | 502 |
| Total | 582 | 732 |

Table 2: Twenty-year survival status categorized by age and smoking habits at the time of the original survey

| Survival <br> status | Age group (years) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 8} \mathbf{- 4 4}$ |  | 44 - 64 |  | above 64 |  |
|  | Smoker | Non- <br> smoker | Smoker | Non- <br> smoker | Smoker | Non- <br> smoker |
| Dead | 19 | 13 | 78 | 52 | 42 | 165 |
| Alive | 269 | 327 | 167 | 147 | 7 | 28 |
| Total | 288 | 340 | 245 | 199 | 49 | 193 |

1. Using Table 1, find the percentage of smokers who survived to the second study.
2. Using Table 1, find the percentage of non-smokers who survived to the second study.

Notice the percentage of smokers who survived is higher than the percentage of nonsmokers who survived. This seems to indicate smoking actually improves the chances of survival. Let's look closer.
3. Using Table 2, find the percentage of smokers who survived to the second study for each individual age group. Do the same for the non-smokers. Record your percentages below in the table provided.

| Age group | $18-44$ | $44-64$ | above 64 |
| :---: | :---: | :---: | :---: |
| Percent of smokers <br> who survived |  |  |  |
| Percent of non- <br> smokers who <br> survived |  |  |  |

4. For each age group, compare and discuss the rates of survival for non-smokers and smokers. Why do you think the conclusion (stated at the top of this page) reversed itself? Why would age make a difference?
5. Find the percentage of the smokers that were above 64 as well as the percentage of the non-smokers that were above 64. Do these numbers help to explain the reversal?

Simpson's paradox exemplifies how lurking variables can distort, even reverse, a statistical conclusion. We must always think about lurking variables when we read or perform studies.

